Introduction to Conic Forms – Part II Graphing Format for Circles, Ellipses and Hyperbolas

Part A. Describe the graph of each of the following equations.

1.
$$\frac{(x-5)^{2}}{9} + \frac{(y+2)^{2}}{16} = 1$$
2.
$$\frac{(x+3)^{2}}{1} - \frac{(y+1)^{2}}{9} = 1$$
3.
$$-\frac{x^{2}}{4} + \frac{y^{2}}{9} = 1$$
4.
$$\frac{(x+4)^{2}}{16} - \frac{(y-3)^{2}}{25} = 1$$
5.
$$(x+3)^{2} + (y+1)^{2} = 25$$
6.
$$x^{2} + (y-5)^{2} = 36$$
7.
$$-\frac{(x-6)^{2}}{4} + \frac{(y-3)^{2}}{49} = 1$$
8.
$$\frac{(x-3)^{2}}{20} + \frac{y^{2}}{100} = 1$$
9.
$$x^{2} + y^{2} = 150$$
10.
$$\frac{(x-1)^{2}}{64} - \frac{(y+7)^{2}}{12} = 1$$
11.
$$-\frac{(x+5)^{2}}{4} + \frac{(y+2)^{2}}{81} = 1$$
12.
$$\frac{(x-3)^{2}}{49} + \frac{y^{2}}{9} = 1$$
13.
$$-\frac{(x-8)^{2}}{2} + \frac{(y+2)^{2}}{50} = 1$$
14.
$$\frac{x^{2}}{144} - \frac{(y+5)^{2}}{25} = 1$$
15.
$$(x+6)^{2} + (y+2.5)^{2} = 4$$
16.
$$\frac{(x-4.5)^{2}}{36} - \frac{(y+1)^{2}}{4} = 1$$
17.
$$\frac{(x-2\frac{1}{2})^{2}}{(\frac{49}{4})} + \frac{(y+1\frac{1}{2})^{2}}{(\frac{121}{4})} = 1$$
18.
$$-\frac{(x-1)^{2}}{169} + \frac{(y+6)^{2}}{30} = 1$$

Part B. Use the above data to graph each problem.

Answers to Part A.

1. Ellipse with center (5,-2) $r_x = 3$, $r_y = 4$

2. Horizontal hyperbola with center (-3,-1) $r_x = 1$, $r_y = 3$

3. Vertical hyperbola with center (0,0) $r_x = 2$, $r_y = 3$

4. Horizontal hyperbola with center (-4,3) $r_x = 4$, $r_y = 5$

- 5. Circle with center (-3,-1) and radius = 5
- 6. Circle with center (0,5) and radius = 6

7. Vertical hyperbola with center (6,3) $r_x = 2, r_y = 7$

- 8. Ellipse with center (3,0) $r_x = \sqrt{20}, r_y = 10$
- 9. Circle with center (0,0) and radius = $\sqrt{150}$
- 10. Horizontal hyperbola with center (1,-7) $r_x = 8, r_y = \sqrt{12}$

11. Vertical hyperbola with center (-5,-2) $r_x = 2, r_y = 9$ 12. Ellipse with center (3,0) $r_x = 7, r_y = 3$ 13. Vertical hyperbola with center (8,-2) $r_x = \sqrt{2}, r_y = \sqrt{50}$ 14. Horizontal hyperbola with center (0,-5) $r_x = 12, r_y = 5$ 15. Circle with center (-6,-2.5) and radius = 2 16. Horizontal hyperbola with center (4.5,-1) $r_x = 6, r_y = 2$ 17. Ellipse with center (2¹/₂, -1¹/₂) $r_x = 3^{1}/_2, r_y = 5^{1}/_2$ 18. Vertical hyperbola with center (1,-6) $r_x = 13, r_y = \sqrt{30}$